

# Equilibria of chromate(VI) species in acid medium and *ab initio* studies of these species

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Abstract—The study of the H<sup>+</sup>–CrO<sub>4</sub><sup>2-</sup> system in 3.0 M KCl as ionic medium at 25°C by means of *emf* (glass electrode) and direct calorimetric measurements, in the total Cr<sup>VI</sup> concentration (*B*), average number of H<sup>+</sup> bounds per central group CrO<sub>4</sub><sup>2-</sup> (*Z*), and pH ranges:  $25 \le B \le 100$  mM,  $0 \le Z \le 1.16$  and  $1 \le pH \le 8$ , respectively, indicates the formation of the following complexes H<sub>p</sub>(CrO<sub>4</sub>)<sup>(p-2q)</sup>, stability constants (log  $\beta_{pq}(\pm 3\sigma)$ ) and partial molar enthalpies ( $\Delta H_{pq}(\pm 3\sigma)$  kcal.mol<sup>-1</sup>): HCrO<sub>4</sub>, 5.888(4), -0.6(1); Cr<sub>2</sub>O<sub>7</sub><sup>2-</sup>, 13.900(3), -5.7(1); H<sub>2</sub>CrO<sub>4</sub>, 7.004(7), 1.8(2) and HCr<sub>2</sub>O<sub>7</sub>, 15.007(5), -5.0(1), respectively, according to the general reaction: pH<sup>+</sup>+qCrO<sub>4</sub><sup>2-</sup>  $\rightleftharpoons$  H<sub>p</sub>(CrO<sub>4</sub>)<sup>(p-2q)</sup>, The results previously obtained by Raman spectroscopy for this system are better adjusted when the HCrO<sub>4</sub> species is included. The energies and optimized structures from *ab initio* calculations for the CrO<sub>4</sub><sup>2-</sup>, HCrO<sub>4</sub>, Cr<sub>2</sub>O<sub>7</sub><sup>2-</sup>, H<sub>2</sub>CrO<sub>4</sub> and HCr<sub>2</sub>O<sub>7</sub> species have also been obtained. For the HCrO<sub>4</sub> species the values of bond lengths and angles theoretically calculated are in good agreement with the experimental data of the anion in the crystal structure of the compound (PPh<sub>4</sub>)[Cr<sup>VI</sup>O<sub>3</sub>(OH)]. Finally, correlations between thermodynamic experimental and structural theoretical parameters are discussed. © 1997 Elsevier Science Ltd

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Over the last few years, there has been a renewed interest in the study of the chromate-dichromate system in relation to the formation of chromium(VI)thioester [1] and chromium(VI)-glutathione [2] compounds, which may be involved in the important role of the carcinogenicity and mutagenicity of chromium(VI). In the process of formation of the quoted compounds, the  $HCrO_4^-$  species is implicated. This species is well known in textbooks [3,4]. However, in references [5-7], examining the Raman spectra of chromates, dichromates and chlorochromates in aqueous solution, in the ranges of pH and total chromium(VI) concentration (B)  $11 \ge pH \ge 1$  and  $300 \ge B \ge 3$  mM, the authors deduce that the protonated form of chromate  $HCrO_4^-$  does not exist, although in accordance with a more recent publication

[8], these results need to be reconfirmed by other methods. In reference [9], studying the electronic spectra of aqueous chromium(VI) solutions in the pH range 3–11, the authors conclude that HCrO<sub>4</sub> is spectrophotometrically undetectable. However, Palmer *et al.* [10] have convincingly argued the formation of HCrO<sub>4</sub> from high-pressure, high-temperature Raman studies and new evidences for the existence of the HCrO<sub>4</sub> anion have been reported by other authors [11]. Moreover, recently in reference [12] the crystal structure of (Ph<sub>4</sub>P)[Cr<sup>VI</sup>O<sub>3</sub>(OH)] has been described. In a recent review these disagreements are treated [13].

We have been working for a long time on this question. Also, considerable uncertainty exists about the nature of the orange-red chromium(VI) species [14,15], which can occur in very acidic solutions:  $H_2CrO_4$  and/or  $HCr_2O_7^-$ .

Chromium(VI) does not give rise to the extensive

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and complex series of iso- and heteropolyanions characteristic of the somewhat less acidic oxides of  $V^{V}$ ,  $Mo^{VI}$  and  $W^{VI}$ , perhaps due to the greater extent of multiple bonding (Cr=O) for the smaller chromium ion [3,16], although the Cr-O bond also has ionic character [17]. Moreover, in basic solutions above pH 8 the main species is the tetrahedral yellow chromate ion  $CrO_4^{2-}$ ; in the range  $6 \ge pH \ge 2$ ,  $HCrO_4^{-}$  and the orange-red dichromate ion  $Cr_2O_7^{2-}$ are in equilibrium; and at pHs below 1 the main species is  $H_2CrO_4$ . The equilibria are represented by the following *pK* values: 0.6 and 5.9, as well as the dimerization constant  $k_{22} = 159$  for the reaction (1).

$$2HCrO_4^- \rightleftharpoons Cr_2O_7^{2-} + H_2O \tag{1}$$

Chemical shifts in the <sup>17</sup>O NMR absorptions for the bridging and terminal oxygen of  $Cr_2O_7^{2-}$ , and for HCrO<sub>4</sub> present at equilibrium with  $Cr_2O_7^{2-}$ , has been reported [18]. The broadening of the former signals, and that for the water solvent caused by adding acid were interpreted as arising from the operation of equilibrium (1) catalized by  $H^+$ . In addition, there are several hydrolysis equilibria which have been studied kinetically [16,19]. For reaction (1) the rate constant from left to right is about 2  $M^{-1}$  sec<sup>-1</sup> and for the basic hydrolysis of  $Cr_2O_7^{2-}$  by H<sub>2</sub>O and OH<sup>-</sup>, which are first order in both dichromate and base concentration, the rate constants have values around  $5 \times 10^{-5}$ and  $400 \,\mathrm{M}^{-1}\,\mathrm{sec}^{-1}$ , respectively. Therefore, the behaviour of the Cr<sup>VI</sup> in solution is simpler than other group VI elements, which form polyoxometalates [20] with 7 Mo or 6 W, whose mechanisms of formation are unknown [16].

Whether chromates or dichromates crystallize depends on the pH, the total metal concentration and the cation present. The tetrahedral structure of the anion  $CrO_4^{2-}$  has been confirmed by many single Xray studies. Within the CrO<sub>4</sub><sup>2-</sup> groups the O—Cr—O angles are close to the tetrahedral value and the Cr-O bond distances are essentially equal and close to 1.6 Å. The anion  $Cr_2O_7^{2-}$  consisted of two distorted  $CrO_4$ tetrahedra [16,17,21] with a corner in common; the bridging Cr-O distance is close to 1.8 Å, while the terminal Cr—O bonds are similar to those in  $CrO_4^{2-}$ , and the Cr-O-Cr angles are around 122-139°. In very strong acid media, high chromium(VI) concentrations: 4 and 12.5 M, and large  $CrO_3/Cr_2O_7^{2-1}$ molar ratios: 8.6 and 92.5, respectively, crystalline trichromates and tetrachromates are formed and the structures contain  $Cr_3O_{10}^{2-}$  and  $Cr_4O_{13}^{2-}$  ions composed of three and four CrO<sub>4</sub> tetrahedra, continue the pattern set by the  $Cr_2O_7^{2-}$  ion in having chains of CrO<sub>4</sub> tetrahedra sharing corners [22,23]. At the limit is the CrO<sub>3</sub> oxide, which consist of infinite chains [3] of -O-CrO<sub>2</sub>-O- corner-sharing tetrahedra. The Raman spectra confirm in very acidic solutions the presence of tri- and tetrachromates [6,7].

On the other hand, since the initial Wolfsberg and Helmholz's studies of the electronic structure of tetraoxocomplexes of transition metals with a closed shell [24], several inorganic and organometallic compounds have been the subject of extensive theoretical investigations [25]. However, for the protonated species derived from the  $CrO_4^{2-}$  and  $Cr_2O_7^{2-}$  anions, we have not found any previous references in the literature, with the exception [26] of  $HCrO_4^{-}$ , on energies and optimized structures obtained from *ab initio* calculations. Ozeki *et al.* [27] studied the structures of  $CrO_4^{2-}$ ,  $HCrO_4^{-}$ ,  $H_2CrO_4$  and  $Cr_2O_7^{2-}$  in aqueous solution using the UV-vis absorption spectra and optimizing these structures so that UV-vis absorption spectra reproduced from molecular orbital calculation DV-X $\alpha$  are fitted to the experimentally obtained component spectra.

We now analyse the studies carried out in aqueous solution, where  $\text{CrO}_4^{2^-}$  ion gives polynuclear acid complexes  $H_p(\text{CrO}_4)_q^{(p-2q)^-}$ , in the following denoted for brevity by the set (p, q), according to the general reaction (2).

$$p\mathbf{H}^{+} + q\mathbf{Cr}\mathbf{O}_{4}^{2-} \rightleftharpoons \mathbf{H}_{p}(\mathbf{Cr}\mathbf{O}_{4})_{q}^{(p-2q)}$$
(2)

So then, we have for chromium and hydrogen ions the mass balance eqs (3).

$$B = b + \Sigma \Sigma q c_{pq}$$
$$BZ(=H - h + K_w h^{-1}) = \Sigma \Sigma p c_{pq}$$
(3)

Chemical symbols are in roman and concentrations in *italic* type [28]. *H* and *B* represent the total analytical concentrations of H<sup>+</sup> and metal, and *h*, *b* and  $c_{pq}$  are the equilibrium concentrations of H<sup>+</sup>,  $\text{CrO}_4^{2-}$  and complex (p,q), respectively;  $K_w$  is the water dissociation constant, and *Z* is defined as the average number of H<sup>+</sup> bounds per central (metal) group  $\text{CrO}_4^{2-}$  [28,29]. Concentrations and equilibrium constants are expressed in M (moles per litre) and errors are parenthetically given [30].

The first study of the acidification of chromates(VI) in solution using the inert ionic medium method [31-35] was accomplished by Sasaki [15], who made emf (glass electrode) and spectrophotometric UV-vis (374, 390 and 400 nm) measurements in 3.0 M NaClO<sub>4</sub> at 25°C, for the total chromium(VI) concentrations interval  $1 \le B \le 200$  mM, covering the range  $0 \le Z \le 1.17$ . For Z < 1, as it increases, the experimental family of curves Z(pH, B) shift as B and pH  $(= -\log h)$  also increase, which indicates that toward Z = 1, polymerization reactions take place and at least one polynuclear complex forms, since all curves for various chromium(VI) total concentrations do not coincide. Therefore, in the wide range with  $Z \sim 1$ , the predominating species must have the general formula  $(\text{HCrO}_4)_q^{q-}$ . Moreover, in contrast to the above-mentioned authors [5-7], one of these complexes must be  $HCrO_4^-$ , since for low B the curves are seen to approach to the so called mononuclear wall [36], which has the right shape to correspond to equilibrium of  $CrO_4^{2-}$  and  $HCrO_4^{-}$ . Thus, Sasaki [15] confirmed the

( <i>p</i> , <i>q</i> )	Medium	Reaction	$\log \beta_{pq}$	$\Delta H_{pq}$ (kcal/mol)	Ref.
(1,1)	3 M Na(ClO₄)	(2)	5.89(2)	1.08(9)	[15,46]
(2,2)		(2)	13.98(4)	-2.68(4)	[15,46]
		(1)	2.20(2)	-4.8(1)	[15,46]
(1,1)	3 M K(Cl)	(2)	5.91(1)	-0.6(2)	[28,35]
(2,2)		(2)	13.87(3)	-5.7(1)	[28,35]
		(1)	2.05(5)	-4.5(5)	[28,35]
	3 M NaNO <sub>3</sub>	(1)	2.16		[14]
(1,1)	dil	(2)		0.7(4)	[48,49]
(2,2)		(1)		-4.7(3)	[48,49]

Table 1. Stability constants and partial molar enthalpies for the reactions (1) and (2) at 25°C

presence of the HCrO<sub>4</sub><sup>-</sup> and  $Cr_2O_7^{2-}$  complexes, not finding any evidence of other products being detected at pH > 1.5. Using graphical methods, the values of the stability constants  $\log \beta_{pq}(3\sigma)$  obtained by this author were  $\log \beta_{11} = 5.89(1)$ ,  $\log \beta_{22} = 13.98(4)$  and  $\log k_{22} = 2.20(2)$  (Table 1). On the other hand, by using least-squares methods (program Letagrop, vide infra) for the emf data of Sasaki [15], we obtained the values  $\log \beta_{11} = 5.903(4)$ ,  $\log \beta_{22} = 14.009(6)$  and  $\log k_{22} = 2.20(1)$ , with a standard deviation  $\sigma(Z)$ = 0.004, in good agreement with that stability constants, while only assuming the complex  $Cr_2O_7^{2-}$ according to references [5–7], we obtain  $\log \beta_{22} =$ 14.36(6), with a standard deviation  $\sigma(Z) = 0.065$ . Hence, for the emf data of Sasaki [15] the model containing the species  $HCrO_4^-$  and  $Cr_2O_7^{2-}$  gives much better fit than the one only assuming the dimer  $Cr_2O_7^{2-}$ . However, at high acidities, Z goes beyond 1, reaching the limit values Z = 1.2 and pH 0.3, such that some new acid products besides  $HCrO_4^-$  and  $Cr_2O_7^{2-}$  must be formed. Nevertheless, since the small data accuracy due to the high acidity at which the measurements were carried out, in addition to the questionable functioning of the glass electrode in chromic acid solutions [34], it could not be confirmed whether the function Z(pH) was independent of B in this range. In any case, Sasaki [15] proposed two options, namely, the complexes  $HCr_2O_7^{2-}$  with  $\log \beta_{32} \leq 14.6$ , or  $H_2CrO_4$ , with  $\log \beta_{21} \leq 7.1$ . Later on, other authors [14] carried out several studies of Cr(VI) in 0.5 and 1 M NaClO<sub>4</sub> at 25°C; from 1 to 7 M NaClO<sub>4</sub> at 20°C and from 1 to 7 M NaNO<sub>3</sub> at 25°C, in order to obtain more information about the influence of the ionic media and temperature on those reactions.

For that very reason, a few years ago we also studied the H<sup>+</sup>—CrO<sub>4</sub><sup>2-</sup> system using 3.0 M KCl as ionic medium, (a) in equilibrium, through *emf* measurements [35] (glass electrode,  $1 \le B \le 100$  mM,  $0 \le Z \le 1$ ) and by means of enthalpy titrations [37– 40] (50 mM  $\le B \le 200$  mM,  $0 \le Z \le 1.5$ ), respectively, at 25°C, and (b) kinetically, by concentration jump and *emf* chemical relaxation measurements [35– 41] ( $5 \le B \le 100 \text{ mM}$ ,  $0.2 \le Z \le 0.8$ ), at 25 and 5°C. The kinetics data should be discussed elsewhere [42].

The equilibrium data were analyzed using graphical methods [28,29], and by means of the Nernst/Leta [43,44] and Varm/Leta [45,46] versions of the generalized least-squares program Letagrop [47], respectively. This program searches for the combination of physicochemical parameters, such as stability constants  $\beta_{pq}$  or partial molar enthalpies  $\Delta H_{pq}$ , as well as for the systematic errors in total (analytical) concentrations, etc., which respectively should do minimum the least-square sums  $U = \Sigma (Z - Z^*)^2$  or  $U = \Sigma (Q - Q^*)^2$ , being  $Z^*$  and  $Q^*$ , the computed values using the proposed model.

First, the treatment of the earlier *emf* data [35] (Fig. 1) also only shows the formation of the species  $HCrO_4^-$  and  $Cr_2O_7^{-2}$ . The values of the stability constants  $\beta_{pq}(3\sigma)$  obtained were  $\log \beta_{11} = 5.918(9)$ ,  $\log \beta_{22} = 13.86(1)$  and  $\log k_{22} = 2.02(3)$ , with a standard deviation  $\sigma(Z) = 0.004$  (Table 1). The continuous trace curves in Fig. 1 were calculated with



Fig. 1. Z, average number of H<sup>+</sup> bound per chromium(VI) at  $CrO_4^{2-}$  level vs pH at 25°C in 3.0 M KCl. The dotted lines were calculated assuming the species  $Cr_2O_7^{2-}$  (log  $\beta_{22} = 14.2$ , Refs. [5,6]) and the continuous lines were calculated assuming the species HCrO<sub>4</sub><sup>-</sup> and  $Cr_2O_7^{2-}$  (log  $\beta_{11} = 5.918$ , log  $\beta_{22} = 13.86$ , Refs [38–42]).

this model. Like Sasaki's work, as Z increases, the experimental Z(pH, B) data shift as B and pH also increase, which indicates that toward Z = 1 polymerization reactions take place, forming  $(HCrO_4)_q^{p-1}$ complexes. Also here, in contrast to the authors [5-7] already mentioned, one of these species must be  $HCrO_4^-$ , because for low B values the curves approach the mononuclear wall corresponding to the equilibrium between  $CrO_4^2$  and  $HCrO_4^-$  ions. The stability constant  $\beta_{11}$  is similar to Sasaki's value, but not  $\beta_{22}$  and  $k_{22}$ , whose values change only slightly with the ionic medium. Moreover, the dotted lines of Fig. 1 were calculated only assuming the formation of the complex  $Cr_2O_7^{2-}$ , according to references [5–7]. In this case, the value of the corresponding stability constant was  $\log \beta_{22} = 14.2(1)$ , with a standard deviation  $\sigma(Z) = 0.068$ . Therefore, also for these *emf* data [35], the model containing the complexes  $HCrO_4^-$  and  $Cr_2O_7^{2-}$  gives a much better fit than that one after the references [5–7] only assuming the dimer  $Cr_2O_7^{2-}$ .

Second, in the calorimetric studies [37-40] it was observed that for the 0 < Z < 1 range the calorific effect was *exothermic*, while for Z or H/B > 1 (Fig. 2) it was endothermic. For the first Z interval the following partial molar enthalpies  $\Delta H_{pq}(3\sigma)$  were obtained:  $\Delta H_{11} = -0.6(1)$ ,  $\Delta H_{22} = -5.7(1)$  and  $\Delta H'_{22} = -4.7(5)$  kcal/mol [reaction (1)], which may be compared with Muldrow and Hepler's [48,49] and Arnek's [46] values compiled in Table 1. It may be observed that the dimerization heat of reaction (1) is practically independent of the ionic medium, while the formation of the complex  $HCrO_4^-$  and  $Cr_2O_7^{2-}$  is more exothermic in 3.0 M KCl than in the other media, so some kind of interaction between the chromate and the Cl<sup>-</sup> ions [38] must be occurring, for example, the formation of  $CrO_3Cl^-$  ion [7,15,18].

The present work on the H<sup>+</sup>-CrO<sub>4</sub><sup>2-</sup> system gives account on the results of: (1) the analysis of a new series of *emf* data (glass electrode, 25°C, 3.0 M KCl,  $25 \le B \le 100 \text{ mM}, 0 \le Z \le 1.16$ ) carried out in order



Fig. 2. Accumulative heat effect per total volume  $\Sigma Q/(v_0 + v)$ vs the ratio H/B for three enthalpy titrations in 3.0 M KCl at 25°C. The continuous lines were drawn using the partial molar enthalpies calculated in this work.

to obtain more knowledge of the speciation topic for Z > 1, using the version Nernst/Leta [44] of Letagrop [47]; (2) the analysis of the earlier calorimetric endothermic experimental data quoted in [38,39] by means of the version Varm/Leta [45] of Letagrop [46]; (3) the analysis of the results previously obtained by Raman spectroscopy [5,6] using the version Beer/Leta [45,50] of Letagrop [47], which shows that the experimental data of the system  $H^+$ — $CrO_4^{2-}$  fit better when the species  $HCrO_4^-$  is included; (4) the study of the energetic stability of the protonated species of chromate(VI), using ab initio theoretical methods (SFC-MO), with double-zeta valence basis set, incorporating pseudopotentials with EPC (effective core potential) to take into account the internal electrons [51], in particular to study the influence of the protonation of oxygen in the  $CrO_4^{2-}$  and  $Cr_2O_7^{2-}$  anion structure. These calculations were made using the program Gaussian 92 [52]; and (5) the discussion of some correlations between experimental thermodynamic parameters and calculated magnitudes using the above-mentioned theoretical methods.

## EXPERIMENTAL

The reagents and the analytical methods detailed in [35–40], the apparatus itemized in [35,38,53], the emf titration method described in [28,29,53] and the enthalpy titration method outlined in [37,40] were used. Solutions of chromate (Z = 0), dichromate (Z = 1) and hydrochloric acid of the following compositions:  $S_1 = CrO_4^{2-}BM$ ,  $K^+$  3.000 M,  $Cl^-$ (3.000-2B) M, S<sub>2</sub> = Cr<sub>2</sub>O<sub>7</sub><sup>2-</sup> 2B M, K<sup>+</sup> 3.000 M, Cl<sup>-</sup> (3.000 - B) M, T<sub>1</sub> = HCl 0.1000 M, KCl 2.900 M and  $T_2 = HCl 1.000 M$ , KCl 2.000 M, respectively, were prepared. The emf titrations were performed at  $25.00(5)^{\circ}$ C, where known amounts of solution T<sub>1</sub> were successively added with a burette to the solutions  $S_1$ or  $S_2$ , kept in an *emf* cell [28,29,53]. Likewise, the enthalpy titrations were carried out at 25.000(1)°C, by successive additions ( $\nu$  ml) of the solution T<sub>2</sub> from a burette to  $v_0 = 100.0$  ml of the solutions  $S_1$  or  $S_2$ contained in the calorimeter reaction vessel [37,40].

## **RESULTS AND DISCUSSION**

#### Analysis of a new series of emf data (25°C, 3.0 M KCl)

First, *emf* data obtained in this work will be discussed (Figs 3 and 4). In Fig. 3 the values of Z(pH, B) are given in all the interval  $0 \le Z \le 1.16$  studied, while Fig. 4 only presents data for Z > 1.

In the zone Z < 1 the situation is very clear and the Z(pH, B) data display the expected behavior [15,35], that is the formation of the complexes HCrO<sub>4</sub><sup>-</sup> and Cr<sub>2</sub>O<sub>7</sub><sup>2-</sup>, that predominate at Z = 1. The values of the stability constant obtained were  $\log \beta_{11} = 5.888(4)$ ,  $\log \beta_{22} = 13.900(3)$  and  $\log k_{22} = 2.12(1)$ , with a standard deviation  $\sigma(Z) = 0.002$ , in good accord with the



Fig. 3. Z, average number of H<sup>+</sup> bound per chromium(VI) at CrO<sub>4</sub><sup>2-</sup> level vs pH (25°C, 3.0 M KCl). The dotted curves were calculated assuming the species HCrO<sub>4</sub><sup>-</sup>, Cr<sub>2</sub>O<sub>7</sub><sup>2-</sup>, H<sub>2</sub>CrO<sub>4</sub> and HCr<sub>2</sub>O<sub>7</sub><sup>-</sup> with the stability constants log  $\beta_{11} = 5.888$ , log  $\beta_{22} = 13.900$ , log  $\beta_{21} = 7.004$  and log  $\beta_{32} = 15.077$ , respectively.



Fig. 4. Z, average number of H<sup>+</sup> bound per chromium(VI) at CrO<sub>4</sub><sup>2-</sup> level vs pH for acid range (25°C, 3.0 M KCl). The full-draw lines were calculated assuming the species HCrO<sub>4</sub>, Cr<sub>2</sub>O<sub>7</sub><sup>2-</sup>, H<sub>2</sub>CrO<sub>4</sub> and HCr<sub>2</sub>O<sub>7</sub> with the stability constants  $\log \beta_{11} = 5.888$ ,  $\log \beta_{22} = 13.900$ ,  $\log \beta_{21} = 7.004$ and  $\log \beta_{32} = 15.077$ , and the heavy border and dotted border lines correspond to the *mononuclear* and the *dinuclear walls*, respectively.

earlier results, Table 1. The dotted trace curves in Fig. 3 were calculated with these stability constants.

On the other hand, for Z > 1, Fig. 4, data were only obtained up to Z = 1.16 and pH = 1.6, but unlike the results obtained by Sasaki [15], the Z(pH, B) curves, although they practically proceed together, depend on the total concentration of chromium(VI). The *heavy border* line for  $B = 5 \times 10^{-5}$  M correspond to the mononuclear wall [36] above-mentioned, when only the mononuclear HCrO<sub>4</sub> and H<sub>2</sub>CrO<sub>4</sub> complexes predominate, which occurs for very diluted chromium(VI) solutions. Analogously, we shall name as *dinuclear wall* the *dotted border* line for B = 500 mM, i.e. when only the *dinuclear* Cr<sub>2</sub>O<sub>7</sub><sup>-</sup> and HCr<sub>2</sub>O<sub>7</sub><sup>-</sup> complexes exist, which happens to be in very strongly concentrated chromium(VI) solutions. It can be observed that as Z increases, the curves Z(pH, B) shift to the left as B decreases and the pH increases. Since at Z = 1 the complexes  $HCrO_4^-$  and  $Cr_2O_7^{2-}$  predominate, this increase in Z for pH < 3 is obviously due to the protonation of one or both species, to form the cited complexes  $H_2CrO_4$  and  $HCr_2O_7^-$ , in accord with the acid-base reactions (4), estimating values of  $pK \approx 1$ .

$$HCrO_{4}^{-} + H^{+} \stackrel{pK_{21}}{\nleftrightarrow} H_{2}CrO_{4}$$
$$Cr_{2}O_{7}^{2-} + H^{+} \stackrel{pK_{32}}{\nleftrightarrow} HCr_{2}O_{7}^{-}$$
(4)

However, if it is assumed that in addition to  $HCrO_4^-$  and  $Cr_2O_7^{2-}$  species only the acid  $HCr_2O_7^{2-}$ is formed in appreciable amounts, for example, for  $pK_{21} \ll 0$  and  $pK_{32} = 1.0$  values, the family of curves Z(pH, B) would take the form represented in Fig. 5, where it can be seen that unlike the experimental data, as Z increases, the calculated curves are shifted towards the left as pH increases and B decreases, whereas if we assume that it forms only the complex  $H_2CrO_4$  ( $pK_{21} = 1$  and  $pK_{32} \ll 0$ ), the family of curves Z(pH, B) would have the form observed in Fig. S1a, with a behaviour similar to that of the experimental data. Therefore, not only the  $HCr_2O_7^-$  species can be expected to be formed, but also H<sub>2</sub>CrO<sub>4</sub> or both complexes. Likewise, the families of curves Z(pH, B) plotted in Figs S1b-S1h were calculated supposing  $pK_{21} = 1.0$ , and  $pK_{32}$  varying from -1.0 to 2.0, respectively. As the value of  $pK_{32}$  increases, the mono- and *dinuclear walls* come closer until for  $pK_{32} = 1.5$  (Fig. S1g), inversion of position takes place. Thus, from this line of argument, it can be concluded that the figure that most closely resembles Fig. 4 (experimental data) is Fig. S1c, with practically equal pK values  $(pK_{21} = 1.1 \text{ and } pK_{32} = 1.0).$ 



Fig. 5. Family of curves Z(pH) in the acid range were calculated assuming that the species  $HCr_2O_7^-$  ( $pK_{32} = 1.0$  and  $pK_{11} \ll 0$ ) is only formed. The heavy border and dotted border lines, respectively correspond to the *mononuclear* (B = 0.05 mM) and the *dinuclear walls* (B = 500 mM).

The same conclusion is also reached supposing that for B = 100 mM and B = 25 mM, only the complexes  $HCr_2O_7^-$  and  $H_2CrO_4$ , respectively were formed. Plotting the data Z(pH, 100 mM) and Z(pH, 25 mM) in accord with expressions (5a) and (5b), two straight lines were obtained with a slope  $\approx 1$  and ordinate in

$$\log (2Z-2)/(3-2Z) = pK_{32} - pH$$
 (5a)

$$\log (Z-1)/(2-Z) = pK_{21} - pH$$
 (5b)

the origin  $pK_{32} = 1.28$  and  $pK_{21} = 1.12$ , respectively, Fig. S2. In conclusion, the analysis of the data Z(pH, B) > 1 by graphical methods indicates the formation of the complexes  $H_2CrO_4$  and  $HCr_2O_7^-$ , starting from the species  $HCrO_4^-$  and  $Cr_2O_7^{2-}$ , having similar pK values. Indeed, analysis of the data by means of version Nernst/Leta [44] of Letagrop [47], allowed the following values of stability constants to be deduced:  $\log \beta_{21} = 7.004(7)$  and  $\log \beta_{32} =$ 15.077(5), with a standard deviation s(Z) = 0.002, and values of  $pK_{21} = 1.12$  and  $pK_{32} = 1.18$ . It should be noted that polynuclear complexes such as  $Cr_3O_{10}^{2-}$ and/or  $Cr_4O_{13}^{2-}$  were rejected by Letagrop. The fulldraw lines of Fig. 4 were calculated using these stability constant. Finally, in Fig. 6 are presented the species distribution diagrams for B = 50 mM. It can be observed that the dimers are the more abundant species, as expected, since for Z > 1, the greater part of the experimental data is situated closer to the dinuclear wall than the mononuclear one (Fig. 4).

# Analysis of the endothermic calorimetric data $(25^{\circ}C, 3.0 \text{ M in KCl})$ at Z > 1 using Letagrop

An analysis will be presented below of the calorimetric data with H/B > 1, Fig. 2 by means of the version Varm/Leta [45] of Letagrop [46]. The best fit was achieved assuming the formation of the H<sub>2</sub>CrO<sub>4</sub> and HCr<sub>2</sub>O<sub>7</sub><sup>2-</sup> complexes, in addition to HCrO<sub>4</sub><sup>-</sup> and Cr<sub>2</sub>O<sub>7</sub><sup>2-</sup> predominating at Z = 1. The following values of the partial molar enthalpies and stability constants, in accord with [2], were obtained:



Fig. 6. Species distribution diagram as a function of pH for B = 50 mM in 3.0 M KCl at 25°C.



Fig. 7. Accumulative heat effect  $\Sigma Q$  vs pH for the endothermic calorimetric data (25°C, 3.0 M KCl) at Z > 1 and concentration in chromium(VI) B mM. Initial solutions of a and b are referred to K<sub>2</sub>CrO<sub>4</sub>; initial solutions of c, d and e are referred to K<sub>2</sub>Cr<sub>2</sub>O<sub>7</sub>. The unbroken lines were drawn using the partial molar enthalpies determined in this work.

 $\Delta H_{21} = 1.8(2)$ ,  $\Delta H_{32} = -5.0(1)$  kcal/mol,  $\log \beta_{21} = 7.56(3)$  and  $\log \beta_{32} = 15.7(1)$ , with  $\sigma(Q) = 0.16$  cal. The experimental data are plotted in Fig. 7. The unbroken lines were calculated assuming the above parameter values.

Table 2 presents the values of the variations of free energy, enthalpy and entropy for several reactions of chromates. Because the formation of a complex is favoured by positive values of  $\Delta S_{pq}^{\circ}$  and negative values of  $\Delta H_{pq}^{\circ}$ , it can therefore be deduced that the acidification reactions of the chromates in 3.0 M KCl at 25°C is entropy-driven, since for reactions between oppositely charged ions there is a net decreasing of ioning charge, which is normally conducive to positive entropy values, as a result of a great increase on the solvent entropy when it has lost the ordenated arrangement of solvent molecules around the reagents. Contrarily, the condensation of the ion HCrO<sub>4</sub><sup>-</sup> to form Cr<sub>2</sub>O<sub>7</sub><sup>2-</sup> is particularly an enthalpydriven reaction.

On the other hand, in Table 3 we present the values of  $\Delta G^{\circ}$ ,  $\Delta H^{\circ}$  and  $\Delta S^{\circ}$  of the stepwise acidification reactions of the ions  $CrO_4^{2-}$  and  $Cr_2O_7^{2-}$ , for comparative purpose with the corresponding values for molybdates(VI) and vanadates(V) [40]. In general, it can be observed that as the acid becomes stronger  $\Delta G^0$ augments, since for a molecule it is much more easy to lose H<sup>+</sup> as the charge decreases. Moreover, this is greatly favored by the entropy term, whereas the enthalpy term is small and unfavorable, except for the protonation of the ion  $HMoO_4^-$ , whose large negative enthalpy term (-11.1 kcal/mol) has been attributed to the promotion in the coordination of Mo<sup>VI</sup> from four in ion  $HMoO_4^{2-}$ , to six in the octahedral neutral species [54]  $Mo(OH)_6$ . By the way, the condensation of species  $HMoO_4^-$  to form  $Mo_2O_7^{2-}$  never has been observed [54]. Finally, it is noted that the successive acidification protonation of the ion  $CrO_4^{2-}$ , as well as

Table 2. Values of  $\Delta G^{\circ}$ ,  $\Delta H^{\circ}$  and  $\Delta S^{\circ}$  ( $\pm 3\sigma$ ) for several reactions of chromates (25 °C, 3.0 M K (Cl))

Reactions	ΔG <sup>0</sup> kcal/mol	Δ <i>H</i> <sup>0</sup> kcal/mol	$\Delta S^0$ e.u.
$\frac{1}{H^+ + CrO_4^{2-} \rightleftharpoons HCrO_4^{-}}$	-8.06(1)	-0.6(2)	25(1)
$2H^+ + 2CrO_4^{2-} \rightleftharpoons Cr_2O_7^{2-} + H_2O$	-18.92(4)	-5.7(1)	45(1)
$2H^+ + CrO_4^{2-} \rightleftharpoons H_2CrO_4$	-10.31(3)	1.8(2)	41(1)
$3H^+ + 2CrO_4^{2-} \rightleftharpoons HCr_2O_7^- + H_2O$	21.4(1)	-5.0(1)	55(1)
$2HCrO_4^- \rightleftharpoons Cr_2O_7^{2-} + H_2O$	-2.80(5)	-4.5(5)	- 5(2)

Table 3. Values of  $\Delta G^{\circ}$  (kcal/mol),  $\Delta H^{\circ}$  (kcal/mol) and  $\Delta S^{\circ}$  (e.u.) for successive acid-base reactions of chromates (3.0 M K(Cl)), molybdates (1.0 M NaCl), heptamolybdates (3.0 M Na(ClO<sub>4</sub>)) and decavanadates (1.0 M Na(ClO<sub>4</sub>)) at 25°C [40]

	n =	1	2	3
$\overline{\mathbf{H}^{+} + \mathbf{H}_{n-1} \operatorname{CrO}_{4}^{n-3}} \rightleftharpoons \mathbf{H}_{n} \operatorname{CrO}_{4}^{n-2}$	$\Delta G^{\circ}$	-8.06	-2.25	
	$\Delta H^{\circ}$	-0.6	2.4	
	$\Delta S^{\circ}$	25	16	
$\mathrm{H}^+ + \mathrm{H}_{n-1}\mathrm{Cr}_2\mathrm{O}_7^{n-3} \rightleftharpoons \mathrm{H}_n\mathrm{Cr}_2\mathrm{O}_7^{n-2}$	$\Delta G^{\circ}$	-2.5		
	$\Delta H^{\circ}$	0.7		
	$\Delta S^{\circ}$	11		
$H^+ + H_{n-1}MoO_4^{n-3} \rightleftharpoons H_nMoO_4^{n-2}$	$\Delta G^{\circ}$	-4.73	- 5.1	
	$\Delta H^{\circ}$	5.38	-11.1	
	$\Delta S^{\circ}$	34	-20	
$\mathrm{H}^+ + \mathrm{H}_{n-1}\mathrm{Mo}_7\mathrm{O}_{24}^{n-7} \rightleftharpoons \mathrm{H}_n\mathrm{Mo}_7\mathrm{O}_{24}^{n-6}$	$\Delta G^{\circ}$	-6.0	-4.8	-3.4
	$\Delta H^{\circ}$	2.6	0.8	-0.6
	$\Delta S^{\circ}$	29	19	10
$H^{+} + H_{n-1}V_{10}O_{28}^{n-7} \rightleftharpoons H_nV_{10}O_{28}^{n-6}$	$\Delta G^{\circ}$	-7.2	5.2	-2.4
	$\Delta H^{\circ}$	-8.2	1.0	0.5
	$\Delta S^{\circ}$	-3	21	10

that of the  $Cr_2O_7^{2-}$ , is also especially enhanced by the entropy term. The diminution trend of  $\Delta S^{\circ}$  comes together with the anions charge decrease, which reflects the decreasing hydration of the anions as they become protonated and their charge is partially neutralized [46], except for the decavanadates where this tendency fails in the first protonation of the  $V_{10}O_{28}^{6-}$ complex [40].

#### Analysis of the Raman spectra using Letagrop

An analysis of the Raman spectroscopy data [5,6] at the frequencies 846 and 904 cm<sup>-1</sup> (Figs 8 and 9) by means of the Beer/Leta [45,50] version of Letagrop [47] assuming only  $Cr_2O_7^{-}$  [5,6] and both species  $HCrO_4^-$  and  $Cr_2O_7^{-}$ , respectively, is shown in Table 4. For Raman spectral measurements an expression analogous to Beer's law was assumed [55,56]. Since in the reference [5] the work was done for B = 200 mM, which is too high to have enough amounts of  $HCrO_4^-$  due to enhanced dimerization, the fit was almost the same assuming both models (Fig. 8). However, in ref. [6], where instead the work was performed at B = 10 mM, the model considering both species



Fig. 8. Relative intensities of Raman data from Ref. [5] at frequencies 846 cm<sup>-1</sup> and 904 cm<sup>-1</sup> vs pH for B = 200 mM. The curves were calculated assuming the species  $Cr_2O_7^{7-}$ (continuous lines), and  $HCrO_4^-$  and  $Cr_2O_7^{7-}$  (dotted lines) by means of Letagrop.

 $HCrO_4^-$  and  $Cr_2O_7^{2-}$  fits better than only supposing  $Cr_2O_7^{2-}$  (Fig. 9), although the results are not sufficiently good due to the paucity of experimental



Fig. 9. Relative intensities of Raman data from Ref. [6] at frequencies 846 cm<sup>-1</sup> and 904 cm<sup>-1</sup> vs pH for B = 10 mM. The curves were calculated assuming the species  $Cr_2O_7^{2-}$ (continuous lines), and  $HCrO_4^-$  and  $Cr_2O_7^{2-}$  (dotted lines) by means of Letagrop.

data. Moreover, our least-squares calculations of these data are in very good agreement with those obtained by Schwarzenbach and Meier [57].

#### Ab initio calculations

The results of the ab initio calculations of the energies and of the optimized geometries of the species  $CrO_4^{2-}$ ,  $HCrO_4^{-}$ ,  $H_2CrO_4$  and  $HCr_2O_7^{-}$ , the existence of which in aqueous solutions has been confirmed in this work, will be discussed below. The results of the optimization of the geometries are given in Tables 5 and 6. In the case of the anion  $CrO_4^{2-}$  the results obtained in this work are compared with those obtained using another basis, in accord with references [58,59]. The values of Cr-O bond lengths calculated are in better accord with those obtained experimentally for the anion  $CrO_4^{2-}$ , using the basis set above-mentioned, and the same may be said for the anion  $Cr_2O_2^{2-}$ , even if these calculations present severe limitations because the basis is limited and electron correlation has not been included. It can be observed firstly that when the Cr-O bond lengths of the protonated species are compared to those of the non-protonated species, all the lengths decrease with the exception of the Cr-O distance of the oxygen bonded to the hydrogen, which increases; consequently, the OH<sup>-</sup> group must become more labile in the substitution reactions. These results for the

Table 4. Analysis of the Raman spectroscopy data (refs [5,6]) at frequencies 846 and 904 cm<sup>-1</sup> by means of Letagrop only, assuming [5,6]  $Cr_2O_7^{2-}$  and both species  $HCrO_4^{-}$  and  $Cr_2O_7^{2-}$ , respectively

(p,q)				$\log \beta_{pq}$	3σ)		
(1,1)	_		5.86(<6.19)	_		5.80(<6.10)	6.04
(2,2)	13.77 <sup>5</sup>	13.76(5)	13.71(6)	14.5(2)6	14.45(<14.71)	13.78(<14.17)	13.78
B	0.2 M			0.01 M	—		—
μ	1.0		_	0.12	—		—
$\sigma(I)$		0.006	0.006	_	0.016	0.012	
Data	Table 7 [5]			Fig. 2 [6]			Ref. [57]

Table 5. Optimized geometries (in Å and deg.) for  $CrO_4^{2-}$  and  $HCrO_4^{-}$  species

Species	Used bases	$d_{\rm Cr-OT}$	$d_{\rm Cr-OH}$	∠0—Cr—	-O∠Cr—O—H	Energy (a.u.)	Ref.
CrO <sub>4</sub> <sup>2-</sup>	Double-zeta val. with pseudopotentials	1.591		Td		- 309.0614	This work
$CrO_4^{2-}$	3-21G	1.604	_	Td		_	[58]
$CrO_4^{2-}$	Minimum STO			Td		-1327.9192	[59]
CrO <sub>4</sub> <sup>2-</sup>	Extended (double-zeta)		—	Td		- 1329.9148	[59]
$CrO_4^{2-}$	Experimental	1.66		Td			[58]
HCrO₄	Double-zeta val. with pseudopotentials	1.513	1.853	106.57 <sup>a</sup> 111.93 <sup>b</sup>	119.50	- 309.81	This work
HCrO₄	Hehre's extend. bases RHF (3–21 G*)	1.537	1.794				[26]

OT = terminal oxygen,  $d_{Cr-OH}$  = chromium-oxygen distance, where the oxygen is bound to hydrogen atom.

<sup>a</sup> min. angle.

<sup>b</sup> max. angle.

	Table 6. Opti	imized geometries (in	$h^{1}$ Å and deg.) for $H_{2}$	$CrO_4$ , $Cr_2O_7^{2-}$ and $HCr_2$	O <sup>7</sup> species, using dout	le-zeta valence basis se	t with pseudopotentia	ıls
Species	d <sub>Cr-OT</sub>	d <sub>cr-oc</sub>	dcr-0H	20-Cr-0	∠ Cr—0—Cr	∠ Cr—O—H	Energy (a.u.)	Ref.
H <sub>2</sub> CrO <sub>4</sub>	1.434		1.745	$108.69^{a}$ 110.66 <sup>b</sup>	-	133.51	-310.3292	This work
CrO,O <sup>2</sup> -	1.513	1.819			139.2	ų	-543.4611	[11]
Cr, 0 <sup>2-</sup>	1.56-1.64	1.76-1.81		-	122-139	1	Ι	Experimental, 21
$HCr_2O_7^-$	1.485	1.912 1.628	1.795	106.50 <sup>a</sup> 112.00 <sup>b</sup>	162.6	123.1		This work
OT = terminí <sup>a</sup> min. angle. <sup>b</sup> max. angle.	ll oxygen, O <sub>c</sub> = cent	ral oxygen; d <sub>cr-oH</sub> =	chromium–oxygen (	listance, where the oxyg	en is bound to hydroge	n atom.		

 $HCrO_{4}^{-}$  anion are in good agreement with those obtained for the anion in the crystal structure [12] of the compound (Ph<sub>4</sub>P)[Cr<sup>v1</sup>O<sub>3</sub>(OH)]. Thus, three Cr-O short bond distances: 1.54, 1.55 and 1.58 Å (theoretical value 1.513 Å, Table 5) and one Cr-O (hydroxy) long bond distance: 2.02 Å (theoretical value 1.853 Å, Table 5) are found, whereas the O-Cr-O bond angles are between 106 and 113° (theoretical values lie between 106.57 and 111.93°, Table 5). The results obtained in the Mulliken population analysis, Table 7, indicate that the oxygen bonded to the proton presents a more negative charge than the remainder of the oxygens. Moreover, it can be seen in Table 5 that the anion  $HCrO_4^-$  is more distorted than the species H<sub>2</sub>CrO<sub>4</sub> and this in turn more than the  $CrO_4^{2-}$ , in accord with the values of the O-Cr-O bond angles calculated. Moreover, the anion  $HCr_2O_7^-$  is distorted with respect to the  $Cr_2O_7^{2-}$ ; it is also observed that the distance of the atom of chromium of the HCrO<sub>3</sub> group of the anion  $HCr_2O_7^-$  to the central oxygen atom is 1.628 Å, while that of the chromium atom of the CrO<sub>3</sub> group of the same anion to the central oxygen atom is 1.91 Å. In the HCr<sub>2</sub> $O_7^{2-}$  anion, the two chromium atoms have a different charge, in accord with the Mulliken population analysis calculations given in Table 7. The Cr-O-Cr angle of the anion  $HCr_2O_7^-$  is 162.6°, while the same angle in the anion  $Cr_2O_7^{2-}$  is between 122 and 139° [21].

# Correlations between experimental thermodynamic and calculated ab initio parameters

It seems logical to expect the existence of direct between the experimental correlations thermodynamic parameters ( $\Delta H^{\circ}, \Delta G^{\circ},$  etc.) that characterize a certain reaction and the interatomic bond models involved. Possible correlations for the acid chromates  $HCrO_4^-$ ,  $HCr_2O_7^-$  and  $H_2CrO_4$  between some of these thermodynamic parameters and the calculated values of the bond lengths,  $d_{\rm Cr-OH}$ , the charge of the dissociating proton,  $z_H$  and the optimized energy E, will be discussed below. Some of these magnitudes of interest are presented in Table 8. However, such correlations must be treated with caution, for two basic reasons. The first is that the calculations of molecular models are referred to non-condensed phases at 0 K, other effects having considerable influence above this temperature. The second reason is associated with the influence of the solvent since bond models generally take into account non-solvated species without taking into account the important contribution of the solvatation [60].

Although Huheey, Keiter and Keiter [61] have established that the reaction enthalpies in gaseous phase may not coincide with polar solvents as water, as can be expected in our case, the stability of the species  $HCrO_4^-$  and  $HCr_2O_7^-$  have been determined by us both by means of *ab initio* calculations in non-

Table 7. Atomic charges calculated through a Mulliken population analysis, using doublezeta valence basis set with pseudopotentials

CrO <sub>4</sub> <sup>2-</sup>	HCrO₄	H <sub>2</sub> CrO <sub>4</sub>	$Cr_2O_7^{2-}$	HCr <sub>2</sub> O <sub>7</sub>
Cr+1.047	+1.069	+1.204	+1.455	+1.1158
				+1.2200
$O_T^{a} - 0.762$	-0.517	-0.210	-0.637	-0.4532
O <sub>T</sub> <sup>a</sup>	-0.495	-0.211	-0.660	-0.3341
O <sub>H</sub> <sup>b</sup>	-0.913	-0.849		-0.8698
H	+0.373	+0.457		+0.4154
O <sub>C</sub> <sup>c</sup>			-1.043	-0.8527

 $^{a}O_{T'}, O_{T} = \text{terminal oxygen}.$ 

 ${}^{b}O_{H} = oxygen bound to hydrogen atom.$ 

 $^{c}O_{c} = central oxygen.$ 

Table 8. Values of pK,  $\Delta G^{\circ}$ ,  $\Delta H^{\circ}$ ,  $\Delta S^{\circ}$ ,  $d_{Cr-OH}$ , charge  $z_{H}$  of the acid proton and optimized energy for the species HCrO<sub>4</sub><sup>-</sup>, HCr<sub>2</sub>O<sub>7</sub><sup>-</sup> and H<sub>2</sub>CrO<sub>4</sub>

	рК	ΔG° (kcal	ΔH° /mol)	Δ <i>S</i> ° (e.u.)	d <sub>Cr-OH</sub> (Å)	Z <sub>H</sub>	<i>E</i> (a.u.)
$HCrO_4^- \rightleftharpoons CrO_4^{2-} + H^+$	5.90	8.06	0.6	-25	1.853	0.373	- 309.81
$HCr_2O_7^- \rightleftharpoons Cr_2O_7^{2-} + H^+$	1.18	2.5	-0.7	-11	1.795	0.415	- 544.16
$H_2CrO_4 \rightleftharpoons HCrO_4^- + H^+$ $CrO_4^{2^-}$	1.12	2.2	-2.4	- 16	1.745	0.457	- 310.33 - 309.06
$Cr_2O_7^{2-}$							- 543.46

condensed phase and by *emf*, calorimetric and Raman spectroscopic studies in aqueous solution. Also, for the majority of the cations hydrolytic reactions (7), where protons are split off from the water molecules bonded to the cation  $M^{n+}$ , it seems that

$$q\mathbf{M}^{n+} + p\mathbf{H}_2\mathbf{O} \rightleftharpoons \mathbf{M}_q(\mathbf{OH})_p^{(nq-p)} + p\mathbf{H}^+$$
(7)

the free energy change depends essentially on enthalpy. For the formation of *mononuclear* complexes the process is somewhat analogous to the dissociation of a proton from a free water molecule, for which we have  $\Delta H_w \approx 13.5$  kcal/mol. For example, for the dissociation of the first proton from the ions Hg<sup>2+</sup>, Fe<sup>2+</sup> and Cd<sup>2+</sup> the  $1/p\Delta H^{-H}$  values are 7.2, 11.0 and 13.1 kcal/mol, respectively, reflecting the decreasing M—O bond strength in that order. Combining  $1/p\Delta H^{-H}$  with  $\Delta H_w$ , we have the enthalpy change  $\Delta H^{OH}$  for the reaction (8). For many

$$q\mathbf{M}^{n+} + p\mathbf{OH}^{-} \rightleftharpoons \mathbf{M}_{q}(\mathbf{OH})_{p}^{(nq-p)}$$
(8)

of the hydroxo complexes,  $1/p \Delta H^{OH}$  is around -8(2) kcal/mol, except for Cd<sup>II</sup> and Ni<sup>II</sup> species, which have smaller values, between 0 and -3 kcal/mol [46]. Also, it has been assumed that  $1/p \Delta G^{-H}$  could be considered as a measure of the acidity of the metallic ion, while  $1/p \Delta H^{OH}$ , except for the solvatation energy, could be taken as a measure of the M—O bond energy.

A plot of  $1/p \Delta H^{OH} vs 1/p \Delta G^{OH}$  shows that all hydroxo complexes are situated on a broad band between the isoentropic lines  $1/p \Delta S^{OH} \approx 10-30$  e.u. Such distributions are in agreement with ionic model behaviour, the more acid cations corresponding to the strongest M-O bond [30]. With this in mind, we have first plotted in Fig. S3a, the bond lengths  $d_{Cr-OH}$  vs the charge  $z_H$  of the proton to be dissociated: Cr-O- $H^{z+}$ , both calculated. As expected, the charge of the proton increases as  $d_{Cr-OH}$  decreases. Secondly, the experimental values have been plotted of the enthalpy of dissociation of H<sup>+</sup> for the reactions (9)  $\Delta H_{B-HB}$  as a function of the charge  $z_H$  of the proton to be dissociated:  $Cr-O-H^{z+}$  (Fig. S3b). Also in this case  $z_H$  increases as  $\Delta H_{B-HB}$  becomes more exothermic.

$$HCrO_{4}^{-} \rightleftharpoons CrO_{4}^{2-} + H^{+}$$
$$HCr_{2}O_{7}^{-} \rightleftharpoons Cr_{2}O_{7}^{2-} + H^{+}$$
$$H_{2}CrO_{4} \rightleftharpoons HCrO_{4}^{-} + H^{+}$$
(9)

Moreover, in Fig. S3c,  $\Delta H_{\rm B-HB}$  has been plotted as a function of bond lengths  $d_{\rm Cr-OH}$ . It is observed that  $d_{\rm Cr-OH}$  decrease as the enthalpy become more exothermic. Lastly, there is a direct correspondence between  $\Delta H_{\rm B-HB}$  and  $\delta E_{\rm B-HB}$  (calculated optimized energies for the unprotonated species and of the protonated ones in reactions (9)). In fact, the reactions (9) become more exothermic as  $\delta E_{B-HB}$  decreases.

The correlation between the experimental parameter  $\Delta H_{B-HB}$  and the three calculated magnitudes  $d_{Cr-OH}$ ,  $z_H$  and  $\delta E_{B-HB}$ , is clearly manifest. It can be concluded that the  $\Delta H_{B-HB}$  is an indirect measurement of the Cr—OH bond energy for the species  $HCrO_4^-$ ,  $HCr_2O_7^-$  and  $H_2CrO_4$ .

Supplementary material—Figures S1a–S1h, S2 and S3a–S3c are available from the authors on request.

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